

1-8: Find the absolute maximum and absolute minimum values of f on the given interval.

1. $f(x) = 12 + 4x - x^2$, $[0, 5]$

$f'(x) = 4 - 2x = 0$
 $x = 2$

x	y
0	12
2	16
5	7

abs max of 16 at $x = 2$
abs min of 7 at $x = 5$

2. $f(x) = 2x^3 - 3x^2 - 12x + 1$, $[-2, 3]$

$f'(x) = 6x^2 - 6x - 12 = 0$
 $x = 2, x = -1$

x	y
-2	-3
-1	8
2	-19
3	-8

abs max of 8 at $x = -1$
abs min of -19 at $x = 2$

3. $f(x) = x^3 - 6x^2 + 5$, $[-3, 5]$

$f'(x) = 3x^2 - 12x = 0$
 $x = 0, x = 4$

x	y
-3	-76
0	5
4	-27
5	-20

abs max of 5 at $x = 0$
abs min of -76 at $x = -3$

4. $f(x) = (x^2 - 1)^3$, $[-1, 2]$

$f'(x) = 3(x^2 - 1)^2 \cdot 2x$
 $x = 0, x = \pm 1$

x	y
-1	0
0	-1
1	0
2	27

abs max of 27 at $x = 2$
abs min of -1 at $x = 0$

Absolute Extrema

Day 5 Application of Derivatives

$f(x) = \frac{x}{x^2 - x + 1}, [0, 3]$

$f'(x) = \frac{-x^2 + 1}{(x^2 - x + 1)^2}$

$f'(x) = 0$
 $(x = \pm 1)$ | $f'(x)$ DNE
 none

x	y
0	0
1	1
3	$\frac{3}{7}$

abs max of ~~1~~ at ~~x=1~~

abs min of 0 at x=0

6. $f(t) = \sqrt[3]{t(8-t)}, [0, 8]$

$= 8t^{1/3} - t^{4/3}$

$f'(t) = \frac{8}{3}t^{-2/3} - \frac{4}{3}t^{1/3}$

$= \frac{8}{3t^{2/3}} - \frac{4t^{1/3}}{3}$

$= \frac{8-4t}{3t^{2/3}}$

t	y
0	0
2	7.5595
8	0

$f'(t) = 0$ | $f'(t)$ DNE

$t = 2$ | $t = 0$

abs min of

0 at x=0, 8

abs max of

7.5595

at x=2

$f(t) = 2\cos t + \sin 2t, [0, \frac{\pi}{2}]$

$f'(t) = -2\sin t + 2\cos 2t$

$\sin t = \cos 2t$

$t = .5236$

x	y
0	2
.5236	2.598
$\frac{\pi}{2}$	0

abs min of 0

at $x = \frac{\pi}{2}$

abs max of

2.598 at $x = .5236$

8. $f(x) = xe^{-\frac{x^2}{8}}, [-1, 4]$

$f'(x) = xe^{-x^2/8} \cdot \frac{-2x}{8} + e^{-x^2/8}$

$= -\frac{x^2 e^{-x^2/8}}{4} + e^{-x^2/8}$

$= e^{-x^2/8} \left(-\frac{x^2}{4} + 1 \right)$

$-\frac{x^2}{4} + 1 = 0$

$-x^2 = -4$

$x = \pm 2$

x	y
-1	-0.882
2	1.213
4	.541

abs min of -0.882

at x=-1

abs max of 1.213

at x=2