

Derivatives: Polynomials & Exponential Functions

1-21: Differentiate the Function

1. $f(x) = e^5$ $f'(x) = 0$	2. $f(t) = 2 - \frac{2}{3}t$ $f'(t) = -\frac{2}{3}$	3. $F(x) = \frac{3}{4}x^8$ $F'(x) = 6x^7$
4. $h(x) = (x-2)(2x+3)$ $= 2x^2 - x - 6$ $h'(x) = 4x - 1$	5. $g(t) = 2t^{\frac{3}{4}}$ $g'(t) = -\frac{3}{2}t^{-7/4}$	6. $A(s) = -\frac{12}{s^5} = -12s^{-5}$ $A'(s) = 60s^{-6}$
7. $y = x^{\frac{5}{3}} - x^{\frac{2}{3}}$ $y' = \frac{5}{3}x^{2/3} - \frac{2}{3}x^{-1/3}$	8. $h(t) = \sqrt[4]{t} - 4e^t = t^{1/4} - 4e^t$ $h'(t) = \frac{1}{4}t^{-3/4} - 4e^t$	9. $\sqrt{x}(x-1) = x^{1/2}(x-1) = x^{3/2} - x^{1/2}$ $\frac{dy}{dx} = \frac{3}{2}x^{1/2} - \frac{1}{2}x^{-1/2}$
10. $3e^x + \frac{4}{\sqrt[3]{x}} = 3e^x + 4x^{-1/3}$ $\frac{dy}{dx} = 3e^x - \frac{4}{3}x^{-4/3}$	11. $y = \frac{x^2 + 4x + 3}{\sqrt{x}} = x^{-1/2}(x^2 + 4x + 3)$ $= x^{3/2} + 4x^{1/2} + 3x^{-1/2}$ $y' = \frac{3}{2}x^{1/2} + 2x^{-1/2} - \frac{3}{2}x^{-3/2}$	12. $y = \frac{\sqrt{x+x}}{x^2} = x^{-2}(x^{1/2} + x)$ $= x^{-3/2} + x^{-1}$ $y' = -\frac{3}{2}x^{-5/2} - x^{-2}$
13. $k(r) = e^r + r^e$ $k'(r) = e^r + e^r r^{e-1}$	14. $f(x) = x^3 - 4x + 6$ $f'(x) = 3x^2 - 4$	15. $f(t) = 1.4t^5 - 2.5t^2 + 6.7$ $f'(t) = 7t^4 - 5t$
16. $g(x) = x^2(1-2x) = x^2 - 2x^3$ $g'(x) = 2x - 6x^2$	17. $S(p) = \sqrt{p} - p = p^{1/2} - p$ $S'(p) = \frac{1}{2}p^{-1/2} - 1$	18. $S(R) = 4\pi R^2$ $S'(R) = 8\pi R$
19. $y = x^8 + 12x^5 - 4x^4 - 6x + 5$ $y' = 8x^7 + 60x^4 - 16x^3 - 6$	20. $y = \frac{3x^2 - \sqrt{x} + x}{x} = x^{-1}(3x^2 - x^{1/2} + x)$ $= 3x - x^{-1/2} + 1$ $y' = 3 + \frac{1}{2}x^{-3/2}$	21. $u = \sqrt[5]{t} + 4\sqrt{t^5} = t^{1/5} + 4t^{5/2}$ $u' = \frac{1}{5}t^{-4/5} + 10t^{3/2}$

22-24: Find an equation of the tangent line to the curve at the given point.

22. $f(x) = 2x^3 + 6$, $(-1, 4)$ $f'(x) = 6x^2 \Big _{x=-1} = 6$ $y - 4 = 6(x + 1)$	23. $y = \sqrt[4]{x}$, $(1, 1)$ $= x^{1/4}$ $y' = \frac{1}{4}x^{-3/4} \Big _{x=1} = \frac{1}{4}$ $y - 1 = \frac{1}{4}(x - 1)$	24. $y = x^4 + 2x^2 - x$, $(1, 2)$ $y' = 4x^3 + 4x - 1 \Big _{x=1} = 7$ $y - 2 = 7(x - 1)$
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